Last Time:

- alignment
- active learning

Lecture 15

HRI, FALL '26

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This Time:

- uncertainty

Uncertainty in HRI .... beyond what we've seen so far?

So far, we have seen a lot of uncertainty in HRI problems! The key type of uncertainty has been in the intentions, goals, rewards that a person has in their mind.

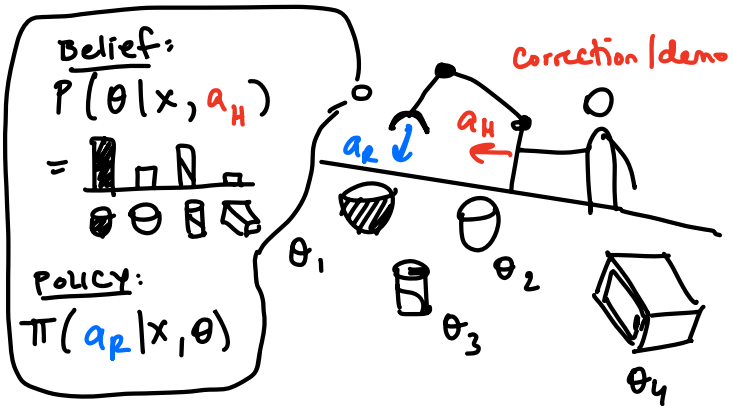
We designed (by hand or via learning algorithms):

$\theta \in \Theta$ // reward/intention parameters

$P(\theta | x, a_H)$ // belief given data (from human)

intent ← θ; x ← state of world; a_H ← human data

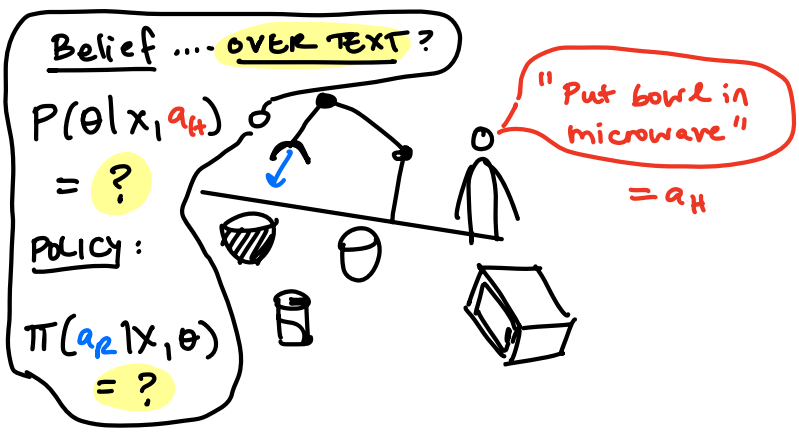
SO FAR



$\theta \in \Theta$ = { θ_1, θ_2, θ_3, θ_4 }

(object poses)

NEXT UP



$\theta \in \Theta$ = { "put metal in microwave", "put ceramic in microwave", "put can in microwave", "pick up microwave", ... }

Q1 How to get $P(\theta | x, a_H)$ when everything is in text?

↳ x = "on the table there is metal bowl, ceramic, ..."

θ = possible things human wants R to do (ex. "put the can in microwave")

a_H = task description from H (ex. "put bowl in microwave")

A1 Lets use a foundation model (LLM)!

1) Let Θ be a finite number of textual descriptions of what the robot could do in this env:

2) Pose a multiple choice Q & A problem to a LLM:

PROMPT:

Human: "put bowl in microwave"
State: There is metal, ceramic....
Which is best?
(A) "put metal in microwave"
(B) "put ceramic in microwave"
(C) "put can in microwave"
(D) "pick up microwave"

→ LLM →

ex. softmax of logits or self-reported!

(A) 0.65 → most likely
(B) 0.2
(C) 0.1
(D) 0.05

$= P_{LLM}(\theta | x, a_R)$

Call a language-conditioned policy to execute:

$\pi(a_R | x, \theta = (A) = \text{"put metal in microwave"})$



⚠ wait, something isn't right!

Q2 What went wrong?

"put bowl in microwave" ⇒ ambiguous if:  or θ ⇒

These should be equally likely!

A) "put metal in microwave"
B) "put ceramic in microwave"

(or maybe bias towards ceramic)

IDEALLY: The robot would accurately know that (A), (B) are both likely and ask for help:



A2 The LLM's "belief update" $P_{LLM}(\theta | x, a_R)$ is miscalibrated! We cannot trust the probabilities!

B/c the LLM is pre-trained (& closed-source and/OR LARGE), it's super hard to change the way it assigns probabilities by retraining, ensembling etc... ☹

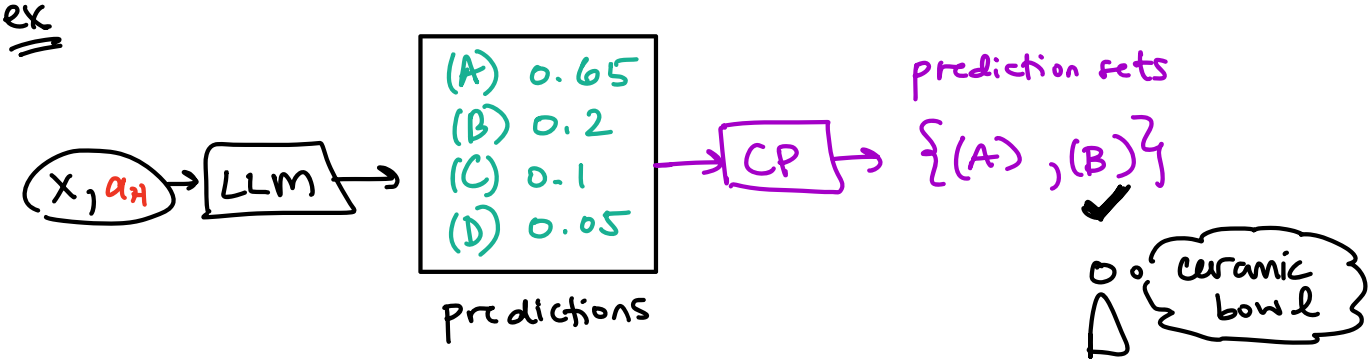
IDEA (from Ren et al, CoRL 2023): Let's use a technique called conformal prediction to ensure that these types of robots "know when they don't know".

CONFORMAL PREDICTION (CP) (Vovk, 2005)

This is a deep topic in statistics and all the proofs on why it works are outside the scope of the class. BUT, the idea + algorithm are quite straightforward:

IDEA Lets take an unreliable predictive model & construct prediction sets which include the true label in the set with high probability.

ex



⇒ if set sz = 1 → execute! if set sz > 1 → ask Q!

Conformal Prediction (CP) ensures that:

$$C(x^{test}, a_H^{test}) \quad \text{s.t.} \quad P(\theta^* \in C(x^{test}, a_H^{test})) \geq 1-\alpha$$

- $C(x^{test}, a_H^{test})$: set of labels (ex. {(A), (B)})
- $P(\theta^* \in C(x^{test}, a_H^{test}))$: probability that true label (θ^*) is in the set ...
- $1-\alpha$: ... is at least $1-\alpha$!
- α: error tolerance!
  - ex. $\alpha = 0.2$ then 80% of the time, true label should be in set C!

even when we can't trust P!

5 STEPS TO CP

⊛ see code ex!

① collect a calibration dataset of inputs & labels:

$$\mathcal{D}_{calib} = \{((x, a_H), \theta^* = (B))\}$$

("put ceramic bowl in microwave" → inputs; (B) → labels)

② Run your predictive model on all inputs in $\mathcal{D}_{calib}$ & measure how badly it mis-predicted!

⇒ prediction: $P_{LLM}(\theta = (B) \mid x, a_H) = 0.2$ ← true label

⇒ mis-prediction score: $1 - P_{LLM} = 0.8$ // higher the score, worse the prediction!

③ choose your error tolerance: α

(ex. $\alpha = 0.2$ means I'm ok not including θ^* in the set 20% of the time)

④ look @ the empirical distribution of $\mathcal{D}_{calib}$ scores and find $\hat{q}$, which is the $\lceil (N+1)(1-\alpha) \rceil / N$ empirical quantile of the scores.

⚠ why this works is out of class scope!

NOTE: Computing plain $1-\alpha$ empirical quantile is bit too optimistic, b/c test point (x^{test}, a_H^{test}) is new pt. we didn't see in $\mathcal{D}_{calib}$.

$\Rightarrow$ Using $\lceil (N+1)(1-\alpha) \rceil / N$ empirical quantile (i.e. $\lceil (N+1)(1-\alpha) \rceil^{th}$ smallest score) accounts for this xtra point at test-time!

(5) At deployment time, the robot carries around $\hat{q}_f$ and constructs the prediction set by including all labels that the predictor (P_{LLM}) is @ least $1-\hat{q}_f$ confident in:

$$C(x^{test}, a_H^{test}) = \{ \theta : P_{LLM}(\theta \mid x^{test}, a_H^{test}) \geq 1 - \hat{q}_f \}$$

In Ren et al, CoRL 2023, the assumption was that any option the LLM was choosing from ((A) – (D)), it could perfectly execute – only uncertainty was semantic.

BUT THIS IS STRONG ASSUMPTION!

ex. Imagine you learn (via VLA) a low-level policy

$$a \sim \pi(a \mid o, \ell)$$

Sometimes the model fails, sometimes the request ℓ is outside of robot's capabilities (ex. π trained on pick + place and ℓ = "pour some milk").

Yuan*, Wu*, Bajcsy. RSS 2026 Handles this!

Supplementary Notes:

Def^n: The α-quantile is the smallest x s.t.

$$P(X \leq x) \geq \alpha$$

(P: cumulative dist. function over rand. variable X)

EXAMPLE: Assume 10 scores, sorted:

$\alpha = 0.75$

0.02, 0.05, 0.08, 0.10, 0.15, 0.3, 0.45, 0.55, 0.7, 0.9

$\alpha = 0.5$ $\alpha = 0.8$

- empirical median ($\alpha = 0.5$): $\lceil 10 \times 0.5 \rceil = 5^{th}$ smallest $= 0.15$
  - ↳ 1/2 scores are @ or below value
- empirical 0.8-quantile: $\lceil 10 \times 0.8 \rceil = 8^{th}$ smallest $= 0.55$
  - ↳ 8/10 scores are @ or below value
- empirical 0.75-quantile: $\lceil 10 \times 0.75 \rceil = 8^{th}$ smallest $= 0.55$

→ Here, the CDF $P(X \leq x)$ counts each value once (l/c unique) so each value contributes 1/10 probability mass.

