

collab

[collab.me.vt.edu](http://collab.me.vt.edu)

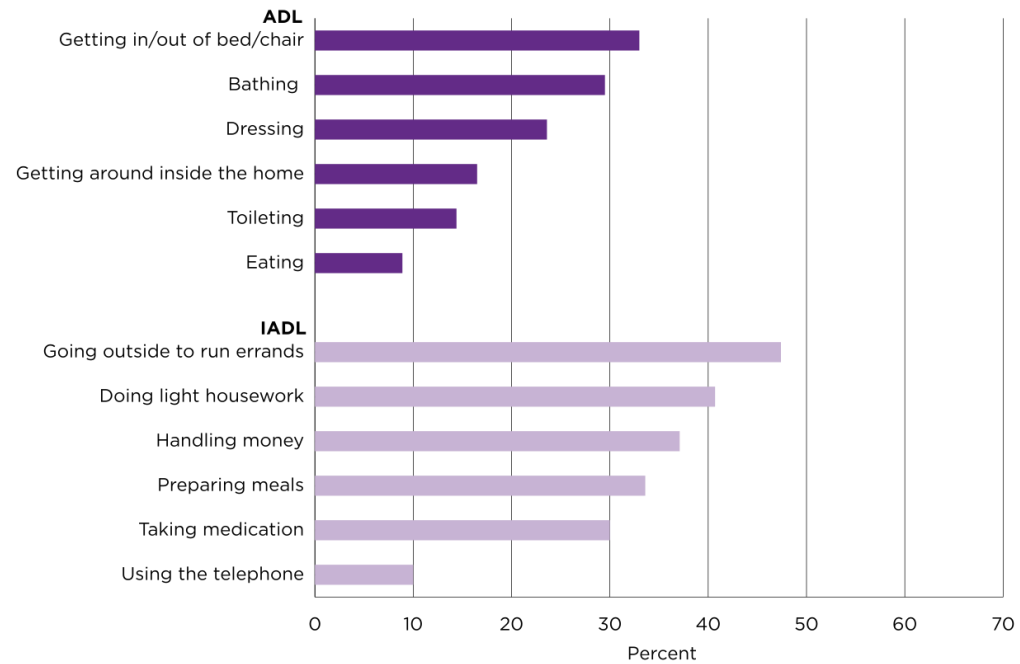
# Shared Autonomy

---

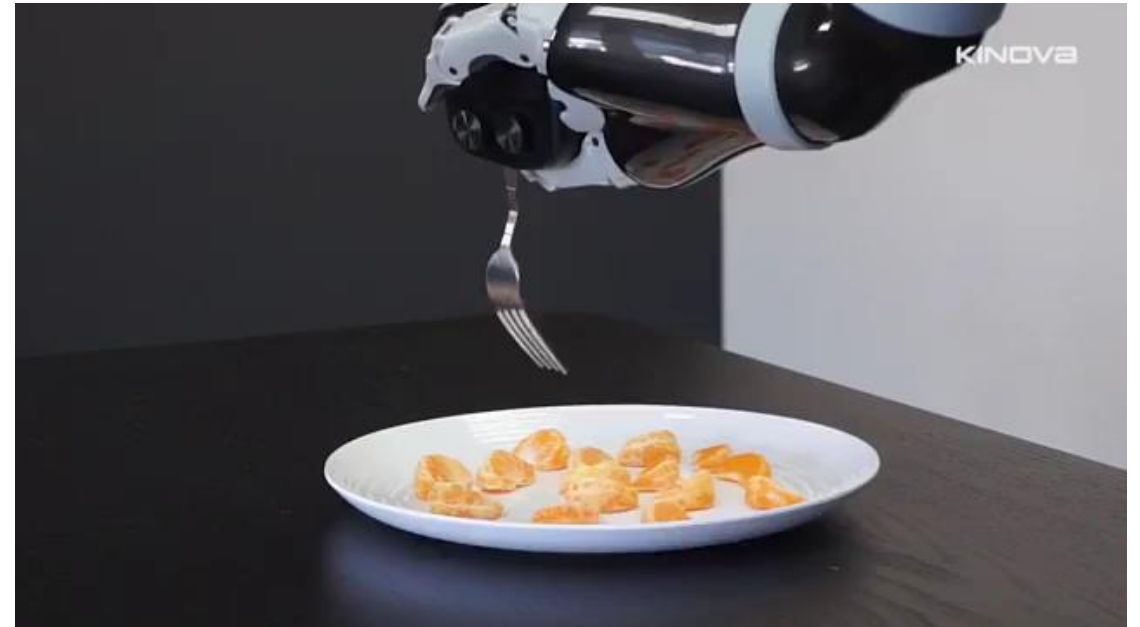
Dylan Losey

Virginia Tech | Fall 2024

**Prevalence of Difficulty Performing ADLs and IADLs in Adults 18 Years and Older With One or More Selected Symptoms That Interfere With Everyday Activities: 2014**



Source: U.S. Census Bureau, Social Security Administration Supplement to the 2014 Panel of the Survey of Income and Program Participation, September-November 2014.







# This Lecture

---

- Introducing shared autonomy
- One flavor of solutions: predicting goals
- Another flavor of solutions: predicting actions

A close-up photograph of a person's face in profile, looking down at a robotic hand holding a strawberry. The scene is dimly lit, with a window blind in the background. The text 'What is shared autonomy?' is overlaid on the image in white and orange.

What is **shared**  
**autonomy**?

# Shared Autonomy

---

Consider a system with:

- State  $s$
- Human input  $u_H$

The system maps the human's input into a commanded action:

$$a_H^t = \phi(s^t, u_H^t)$$



# Shared Autonomy

---



# Shared Autonomy

---

Consider a system with:

- State  $s$
- Human input  $u_H$
- Assistive action  $a_R$

The dynamics depend on both the human's input and the robot's assistance:

$$s^{t+1} = f\left(s^t, a_R^t, \phi(s^t, u_H^t)\right)$$

# Shared Autonomy

---



# Shared Autonomy

---



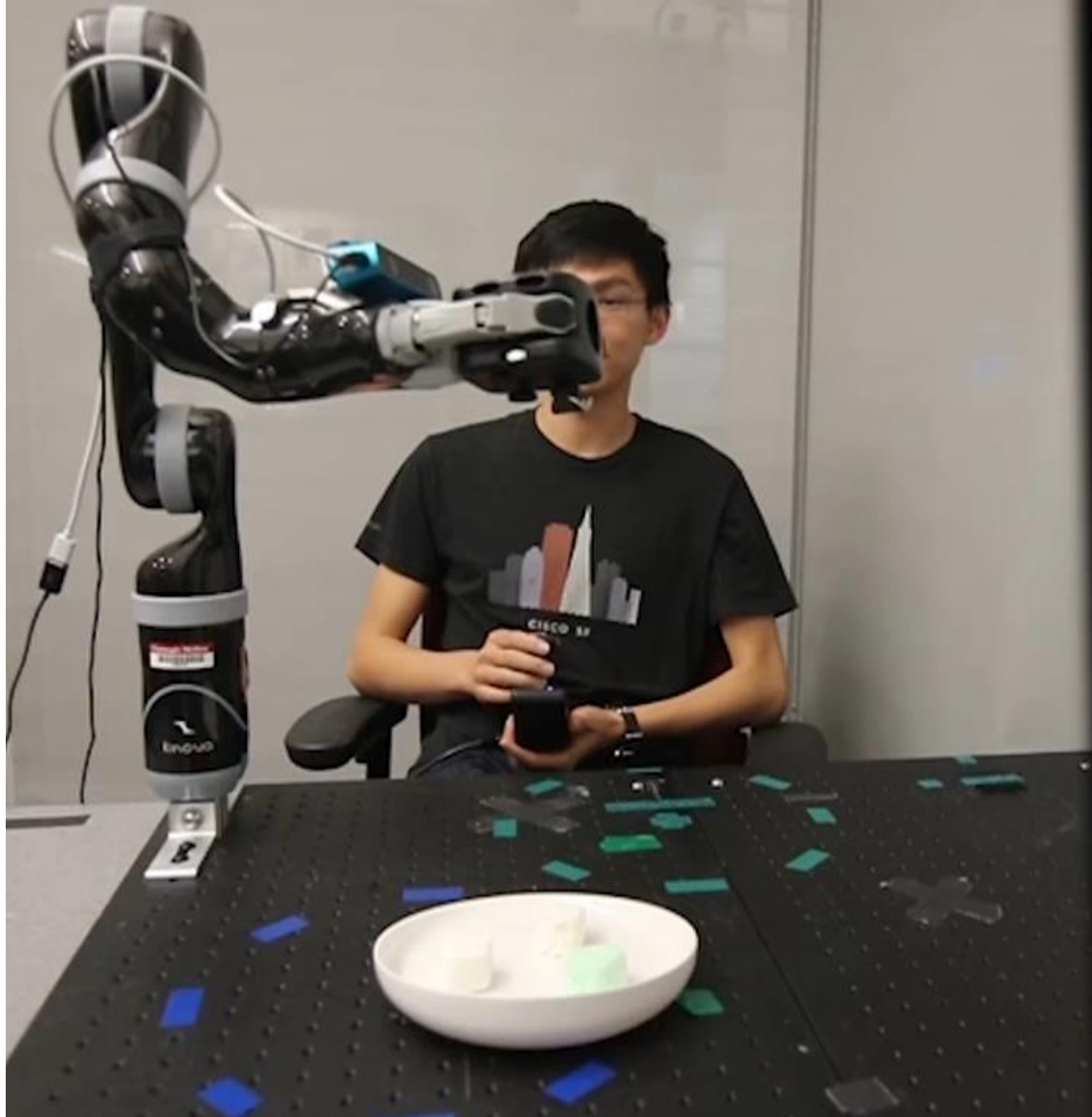
# Shared Autonomy

---



A close-up photograph of a robotic hand holding a single strawberry. The hand is positioned near the face of a young man with dark, curly hair, who is looking towards the strawberry. The background is a window with horizontal blinds. The image is overlaid with a semi-transparent dark grey filter.

# Shared Autonomy: Predicting Goals



Assistive arms  
allow people  
with disabilities  
and robots to  
work together to  
perform tasks,  
like eating.

# Predicting Goals

---

One approach is to think of shared autonomy as an **optimization problem** under uncertainty. The human knows the reward (i.e., the goal), and the robot needs to predict that goal, and take assistive actions towards the goal.

$$\mathcal{M} = \langle S, A_R, U_H, f, \phi, \theta \rangle$$

---

*Shared autonomy written as a Markov decision process (can be extended to POMDP)*



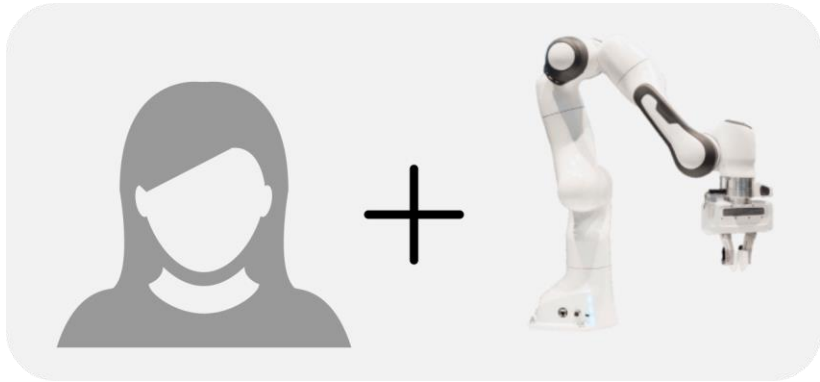
# Predicting Goals

---

$$\mathcal{M} = \langle S, A_R, U_H, f, \phi, \theta \rangle$$

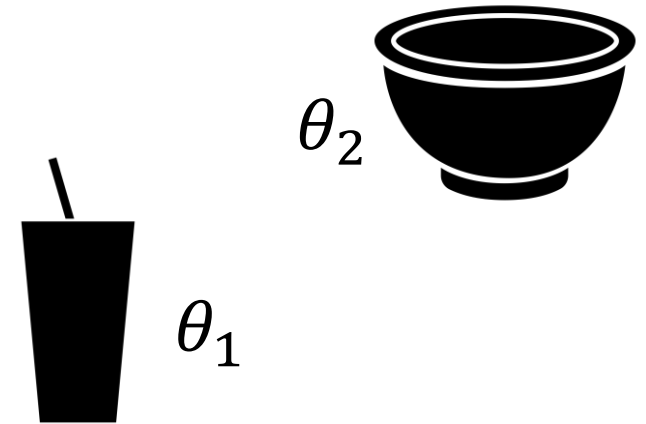
- $S$  is the set of states
- $A_R$  and  $U_H$  are the set of assistive actions and human inputs
- $f$  and  $\phi$  are the known dynamics (including the input mapping)
- $r(s, \theta)$  is the **reward function** that the robot should optimize for
- $\theta$  is the human's goal, which the robot does not know *a priori*

# Predict & Blend



---

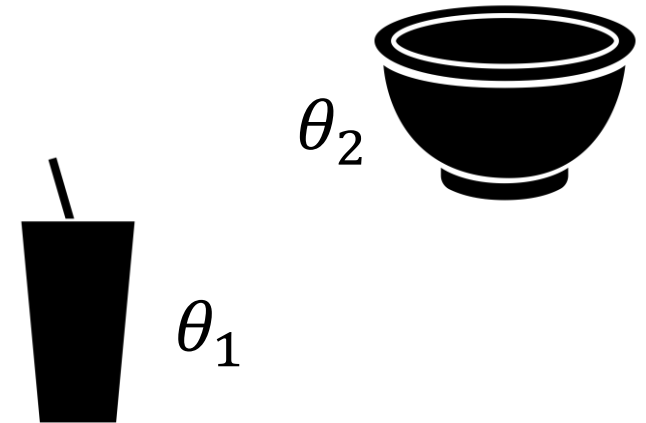
Imagine the human and robot are trying to reach for a **goal** in **free space**.



# Predict & Blend

**Step 1 (Predict):** Infer which goal the human is trying to reach

**Step 2 (Blend):** Blend the human's commanded action with assistive action

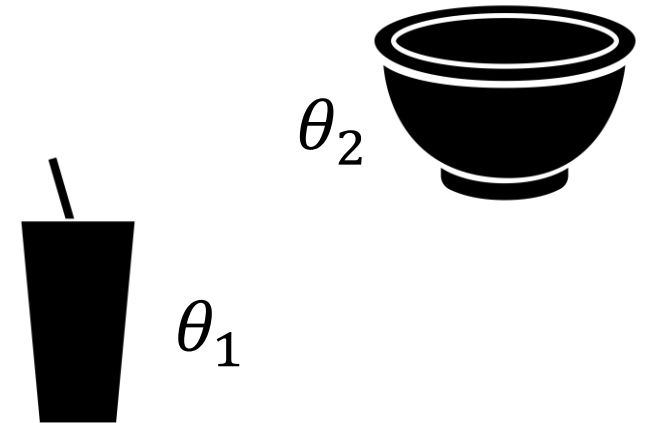


# Predict & Blend

**Step 1 (Predict):** Infer which goal the human is trying to reach



**Step 2 (Blend):** Blend the human's commanded action with assistive action



# Predict & Blend

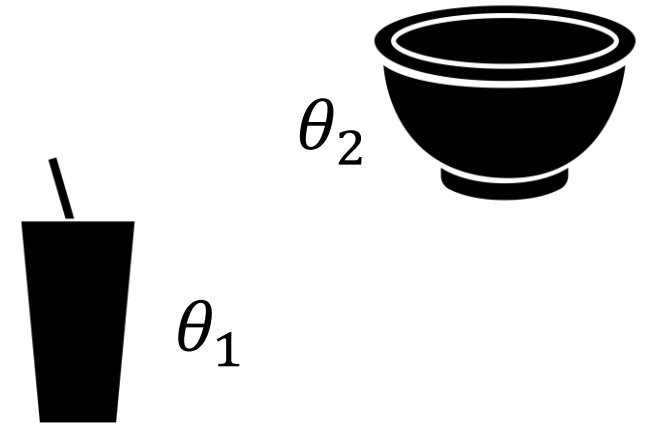
**Step 1 (Predict):** Infer which goal the human is trying to reach

- Start with prior  $P(\theta)$
- At each timestep get  $(s, a_H)$
- Update posterior:

$$P(\theta | D) \propto P(\theta) \prod_{(s, a_H) \in D} P(a_H | s, \theta)$$

---

*Often people simplify this...*



$$s^0 = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$



$$s^t = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

$$\theta_2 = \begin{bmatrix} 8 \\ 3 \end{bmatrix}$$



$$\theta_1 = \begin{bmatrix} 5 \\ 2 \end{bmatrix}$$

$$s^0 = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$



$$s^t = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

### Naïve approach

Probability human wants a goal is inverse prop. to distance from goal

$$P(\theta | D) \propto \frac{1}{\|\theta - s^t\|}$$

↑  
Distance left to  $\theta$



$$\theta_1 = \begin{bmatrix} 5 \\ 2 \end{bmatrix}$$

$$\theta_2 = \begin{bmatrix} 8 \\ 3 \end{bmatrix}$$



$$s^0 = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$



$$s^t = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

### Naïve approach

Probability human wants a goal is inverse prop. to distance from goal

$$P(\theta | D) \propto \frac{1}{\|\theta - s^t\|}$$



$$P(\theta_1 | s^t) = 0.75$$

$$P(\theta_2 | s^t) = 0.25$$





$$s^0 = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$



$$s^t = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

### Better approach

Consider how efficiently human is moving towards the goal

$$P(\theta | D) \propto \frac{\|\theta - s^0\|}{\underbrace{\|s^t - s^0\|}_{\text{Distance gone so far}} + \underbrace{\|\theta - s^t\|}_{\text{Distance left to } \theta}}$$

*Distance gone so far*

*Distance left to  $\theta$*



$$\theta_1 = \begin{bmatrix} 5 \\ 2 \end{bmatrix}$$

$$\theta_2 = \begin{bmatrix} 8 \\ 3 \end{bmatrix}$$



$$s^0 = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$



$$s^t = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

### Better approach

Consider how efficiently human is moving towards the goal

$$P(\theta | D) \propto \frac{\|\theta - s^0\|}{\|s^t - s^0\| + \|\theta - s^t\|}$$



$$P(\theta_1 | s^t) = 0.48$$

$$P(\theta_2 | s^t) = 0.52$$



# Predict & Blend

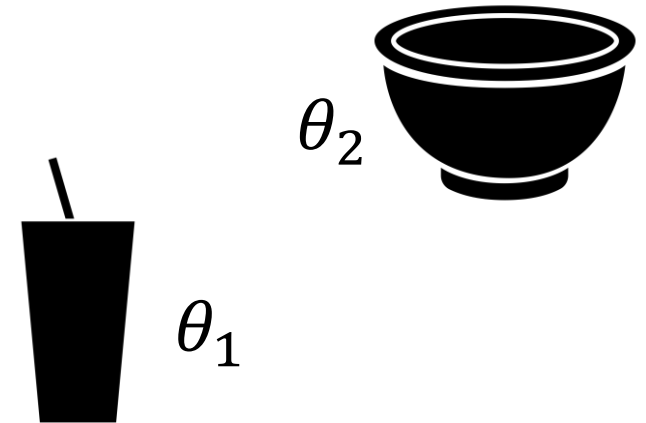
**Step 1 (Predict):** Infer which goal the human is trying to reach

- Start with prior  $P(\theta)$
- At each timestep get  $(s, a_H)$
- Update posterior:

$$P(\theta | D) \propto P(\theta) \frac{\exp(\beta \cdot \|\theta - s^0\|)}{\exp(\beta \|s^t - s^0\| + \beta \|\theta - s^t\|)}$$

---

*One common simplification for free space goals*

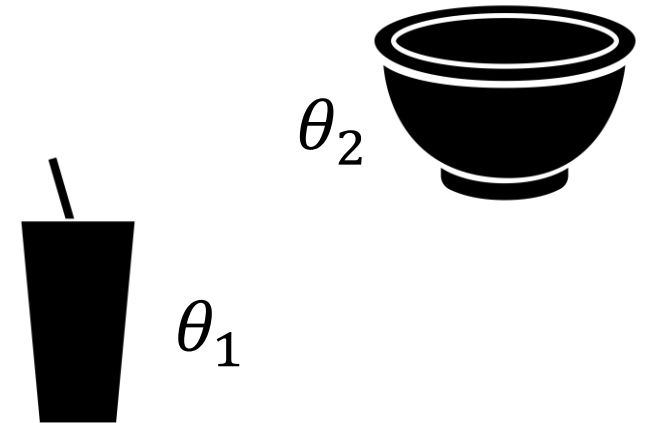


# Predict & Blend

Step 1 (Predict): Infer which goal the human is trying to reach



Step 2 (Blend): Blend the human's commanded action with assistive action

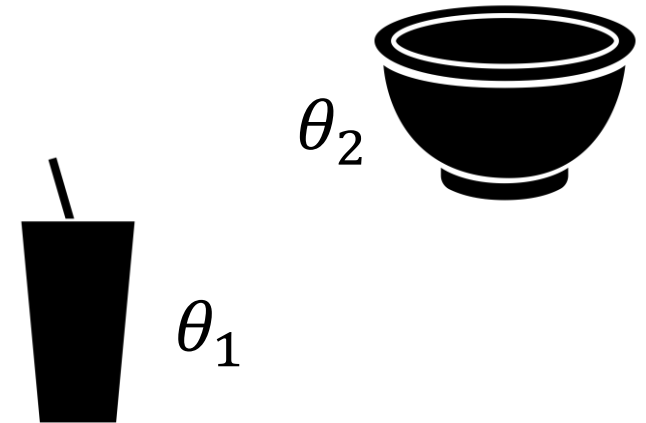


# Predict & Blend

**Step 2 (Blend):** Blend the human's commanded action with assistive action

$$a = (1 - \alpha) \cdot a_H + \alpha \cdot a_R$$

*Linearly blend the human and robot actions,  
the robot executes the overall action  $a$*



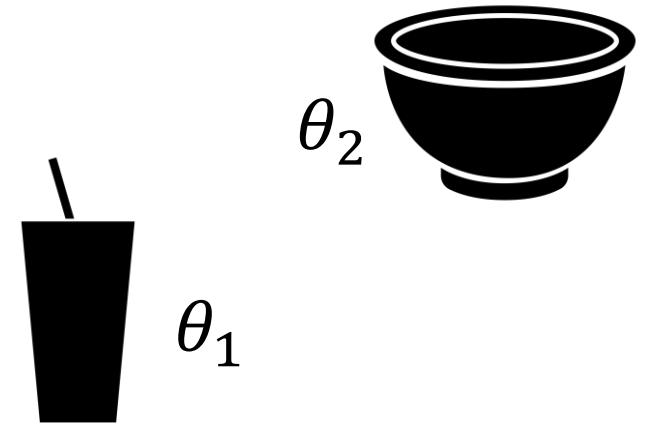
# Predict & Blend

**Step 2 (Blend):** Blend the human's commanded action with assistive action

$$a = (1 - \alpha) \cdot a_H + \alpha \cdot a_R$$

*We know this...*

*What about the assistive  
robot action?*



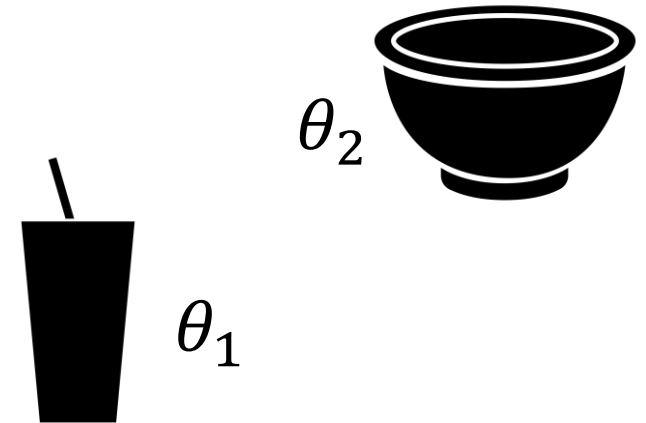
# Predict & Blend

**Step 2 (Blend):** Blend the human's commanded action with assistive action

$$a = (1 - \alpha) \cdot a_H + \alpha \cdot a_R$$

$$a_R = \sum_{\theta \in \Theta} \underbrace{P(\theta|D)} \cdot (\theta - s^t)$$

*Assist towards weighted average goal*



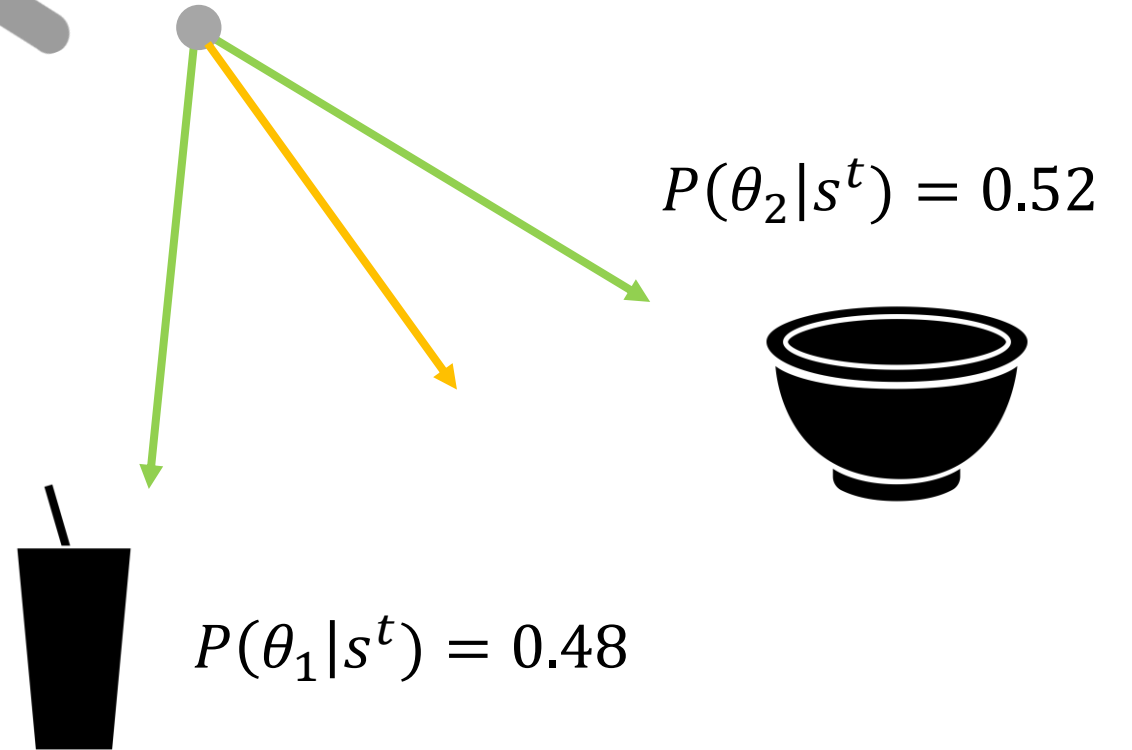


**Step 2 (Blend):** Blend the human's commanded action with assistive action

$$a = (1 - \alpha) \cdot a_H + \alpha \cdot a_R$$

$$a_R = \sum_{\theta \in \Theta} P(\theta|D) \cdot (\theta - s^t)$$

*Assist towards weighted average goal*





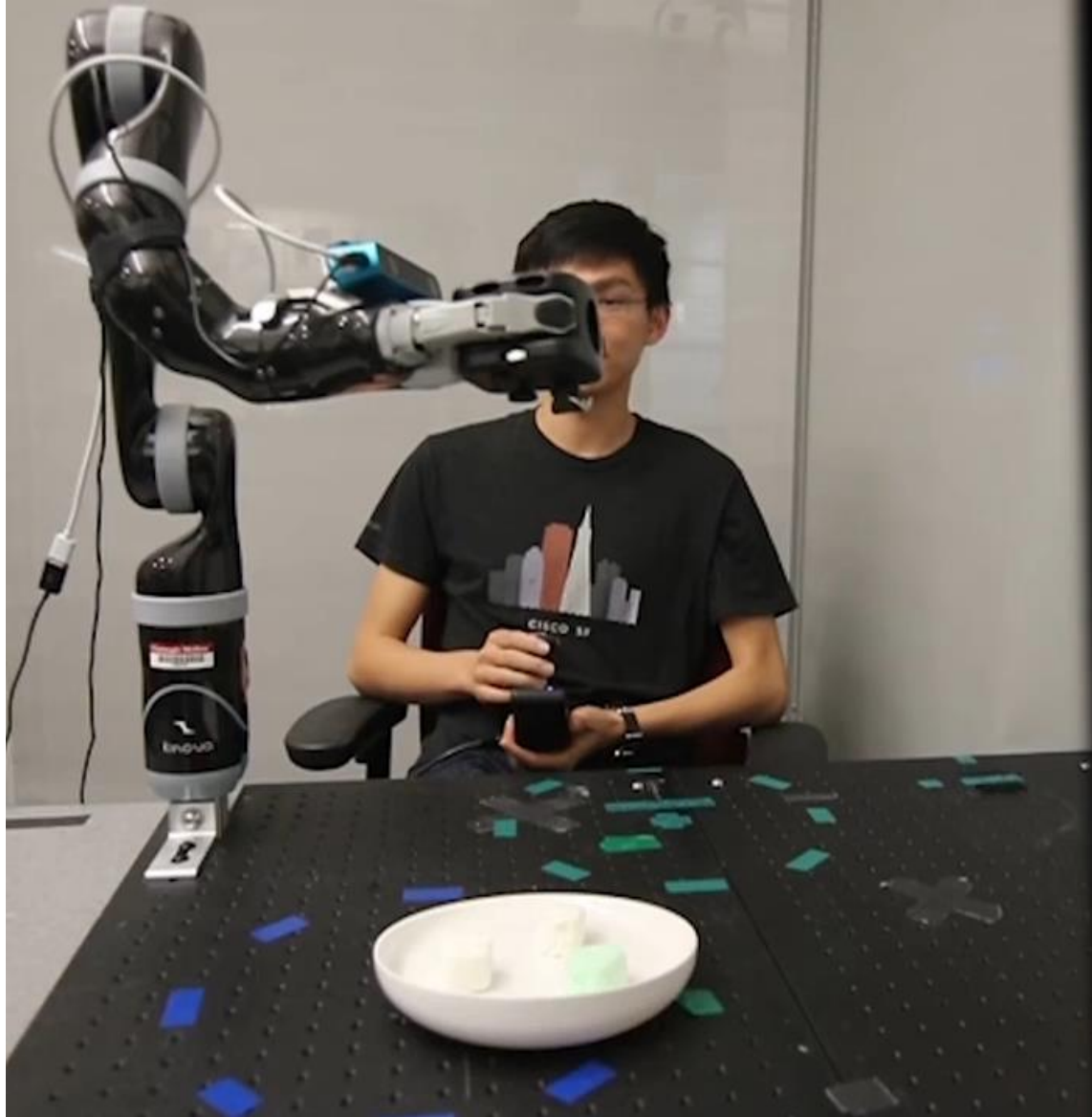
# Predict & Blend

**Given** set of possible goals  $\theta \in \Theta$

**Given** prior over goals  $P(\theta)$

**For** each timestep  $t$

- Measure state  $s$  and human input  $a_H$
- **Predict**  $P(\theta | D) \propto P(\theta) \prod_{(s, a_H) \in D} P(a_H | s, \theta)$
- Compute assistance  $a_R = \sum_{\theta \in \Theta} P(\theta | D) \cdot (\theta - s^t)$
- Take **blended** action  $a = (1 - \alpha) \cdot a_H + \alpha \cdot a_R$



Assistive arms  
allow people  
with disabilities  
and robots to  
work together to  
perform tasks,  
like eating.

# Related Papers

- <https://journals.sagepub.com/doi/full/10.1177/0278364913490324>
- <https://journals.sagepub.com/doi/full/10.1177/0278364918776060>
- <https://dl.acm.org/doi/pdf/10.1145/3359614>

A close-up photograph of a robotic hand holding a single strawberry on a fork. The hand is positioned near the face of a young man with dark, curly hair, who is looking towards the strawberry. The background is a window with horizontal blinds. The image has a dark, semi-transparent overlay.

# Shared Autonomy: Predicting Actions

# Shared Autonomy

---

Consider a system with:

- State  $s$
- Human input  $u_H$

The system maps the human's input into a commanded action:

$$a_H^t = \phi(s^t, u_H^t)$$

# Shared Autonomy

---





The robot autonomy generates trajectory segments



$$a_H = \phi(s, u_H)$$





# Predicting Actions

---

With assistive applications in mind, the human's input is often **low-dimensional**. But the robot the human is trying to control is **high-dimensional**. Instead of assuming access to a discrete set of goals, can we enable the human to seamlessly control their complex and dexterous robot arm?

$$a_H = \phi(s, u_H)$$

---

*These approaches learn a mapping from states and inputs to commanded robot actions*

# Predicting Actions

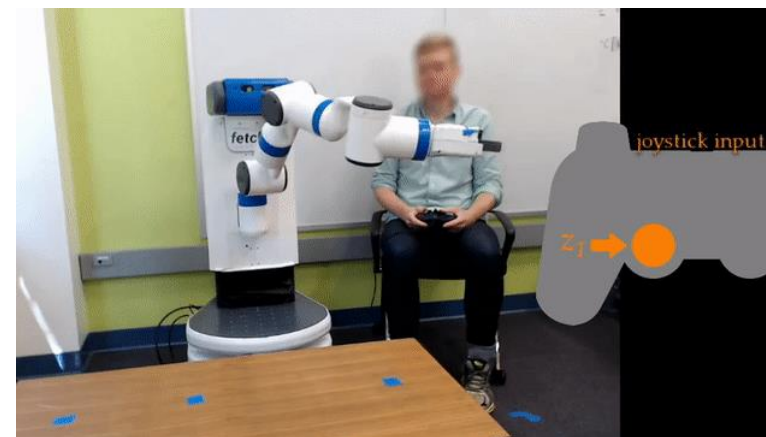
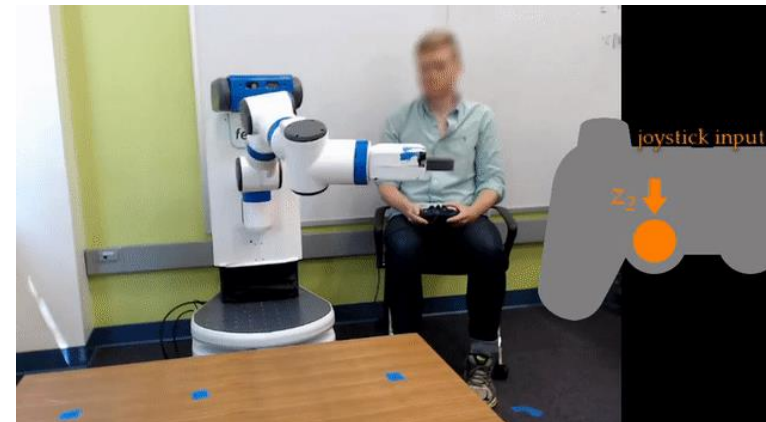
---

$$a_H = \phi(s, u_H)$$

- $s$  is the current state (i.e., joint position + any camera images)
- $u_H$  is the human's low-dimensional input (i.e., 2-DoF joystick)
- $\phi$  is the unknown teleoperation mapping from inputs to actions
- $a_H$  is the **high-dimensional** action the human wants the robot to take



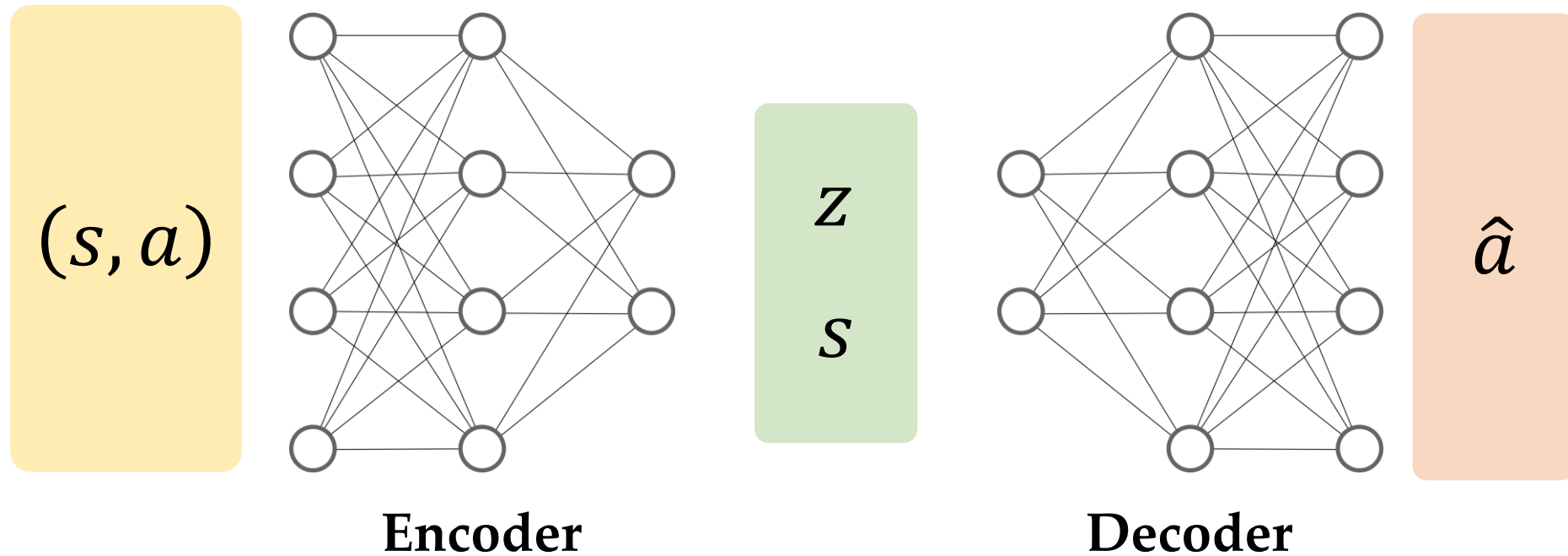
$(s, a)$



$(s, u_H)$

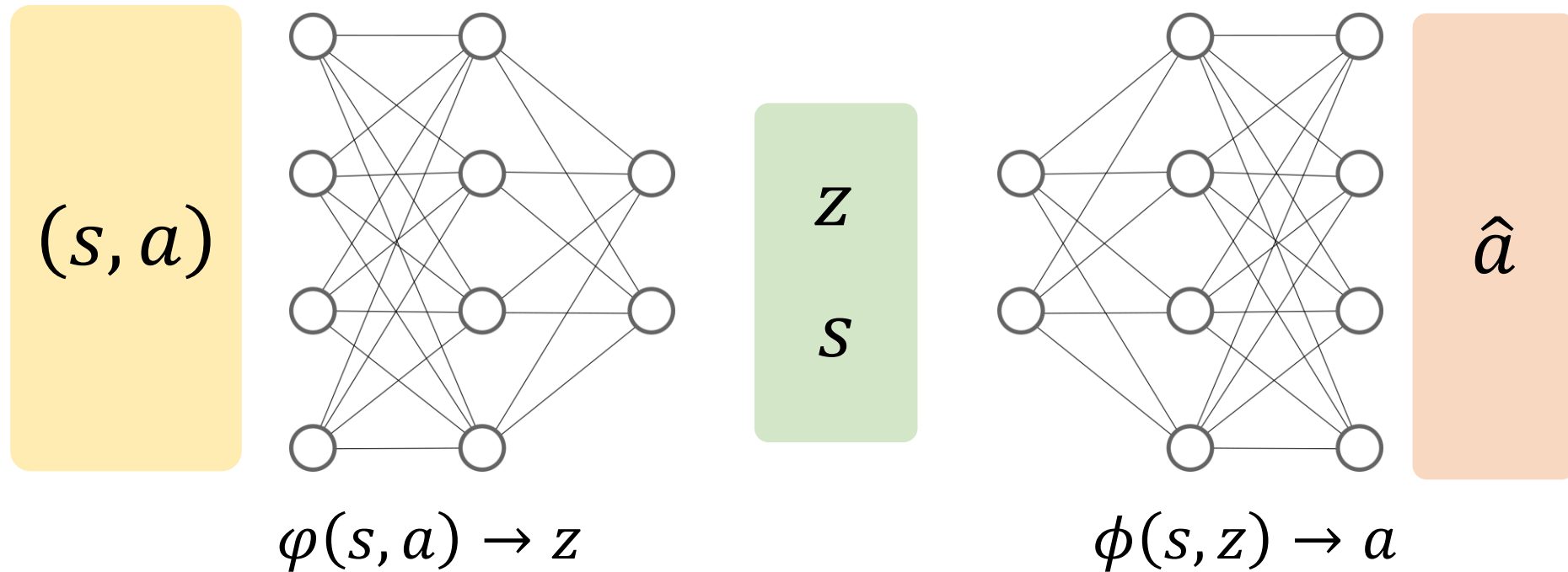
# Latent Actions

To learn the mapping  $\phi(s, u_H) \rightarrow a_H$  we will use a **conditional autoencoder**.



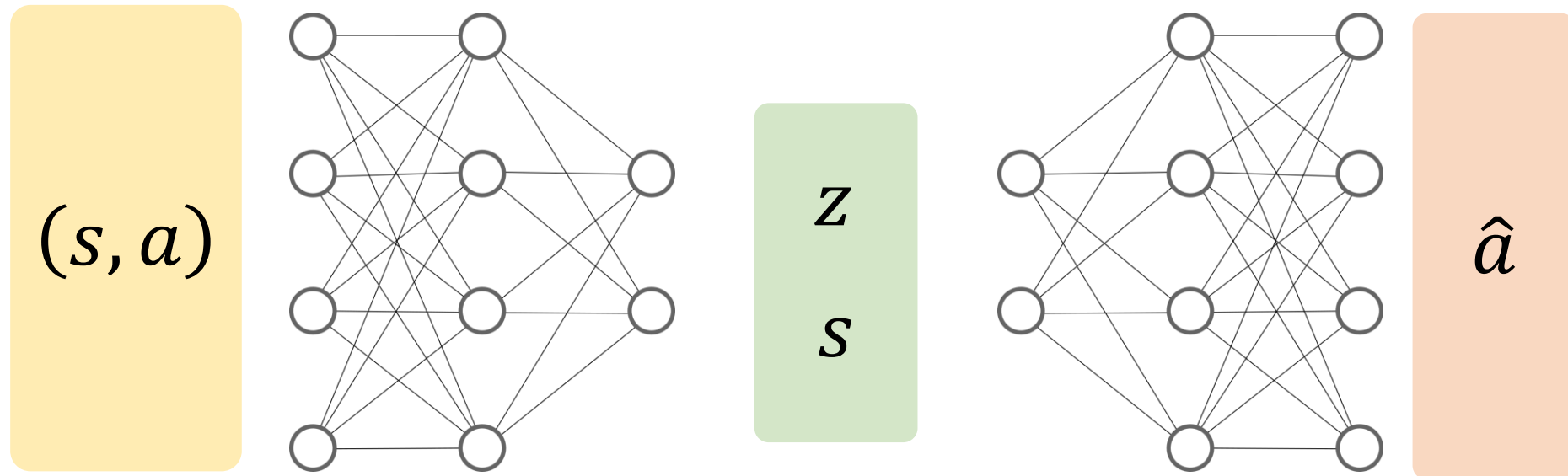
# Latent Actions

To learn the mapping  $\phi(s, u_H) \rightarrow a_H$  we will use a **conditional autoencoder**.



# Latent Actions

To learn the mapping  $\phi(s, u_H) \rightarrow a_H$  we will use a **conditional autoencoder**.



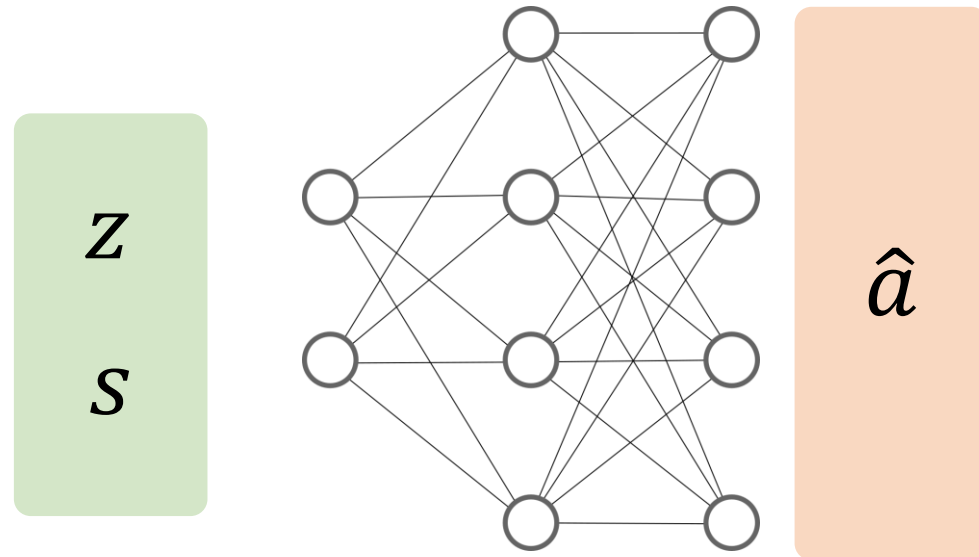
$$\varphi(s, a) \rightarrow z$$

The decoder is *conditioned* on state  $s$ . Take  $s$  from input and pass directly to decoder.

# Latent Actions

To learn the mapping  $\phi(s, z) \rightarrow a$  we will use a **conditional autoencoder**.

Once trained, we control the robot using only the decoder to get action  $a$



# Latent Actions

**Our idea.** We embed high-dimensional and complex tasks to low-dimensional **latent representations**. At runtime users select the latent representation with a joystick, which then maps to high-dimensional and meaningful behaviors.



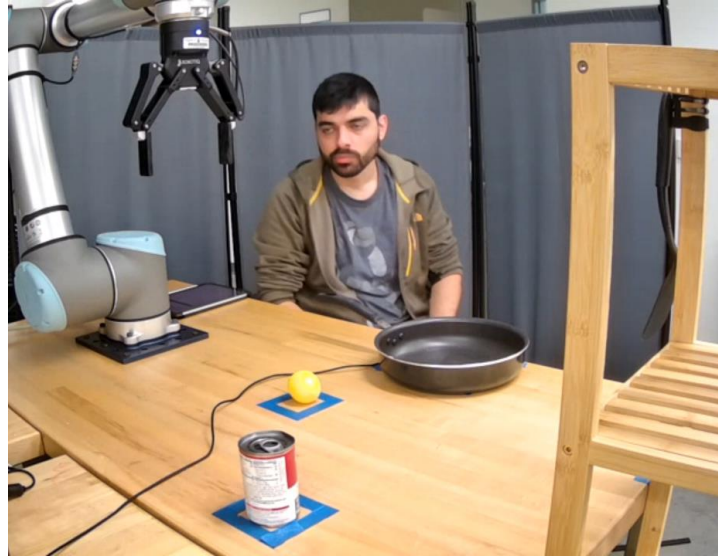
---

*When user presses the joystick to the right, the robot decodes this latent input to help reach the spatula*



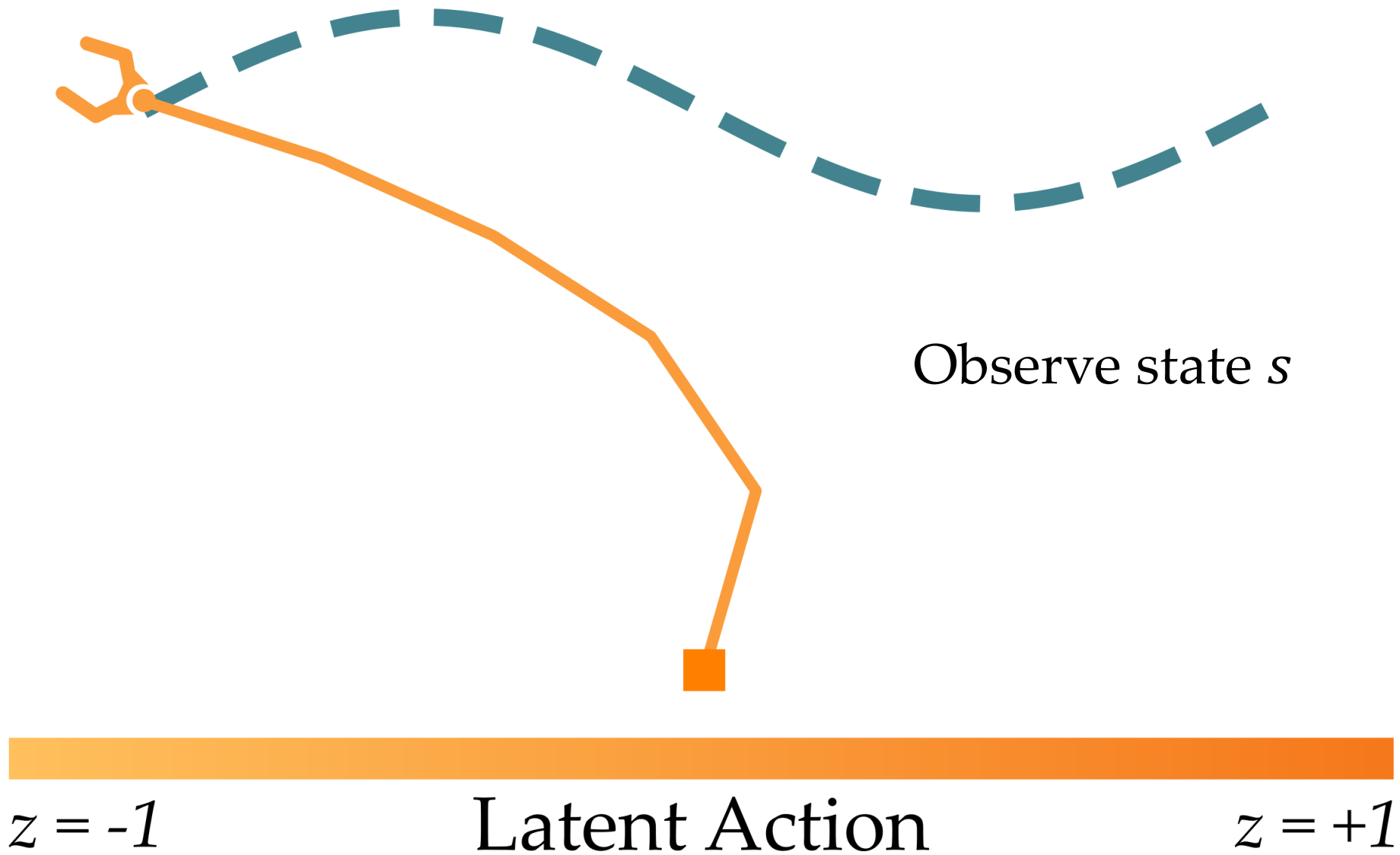
# Latent Actions

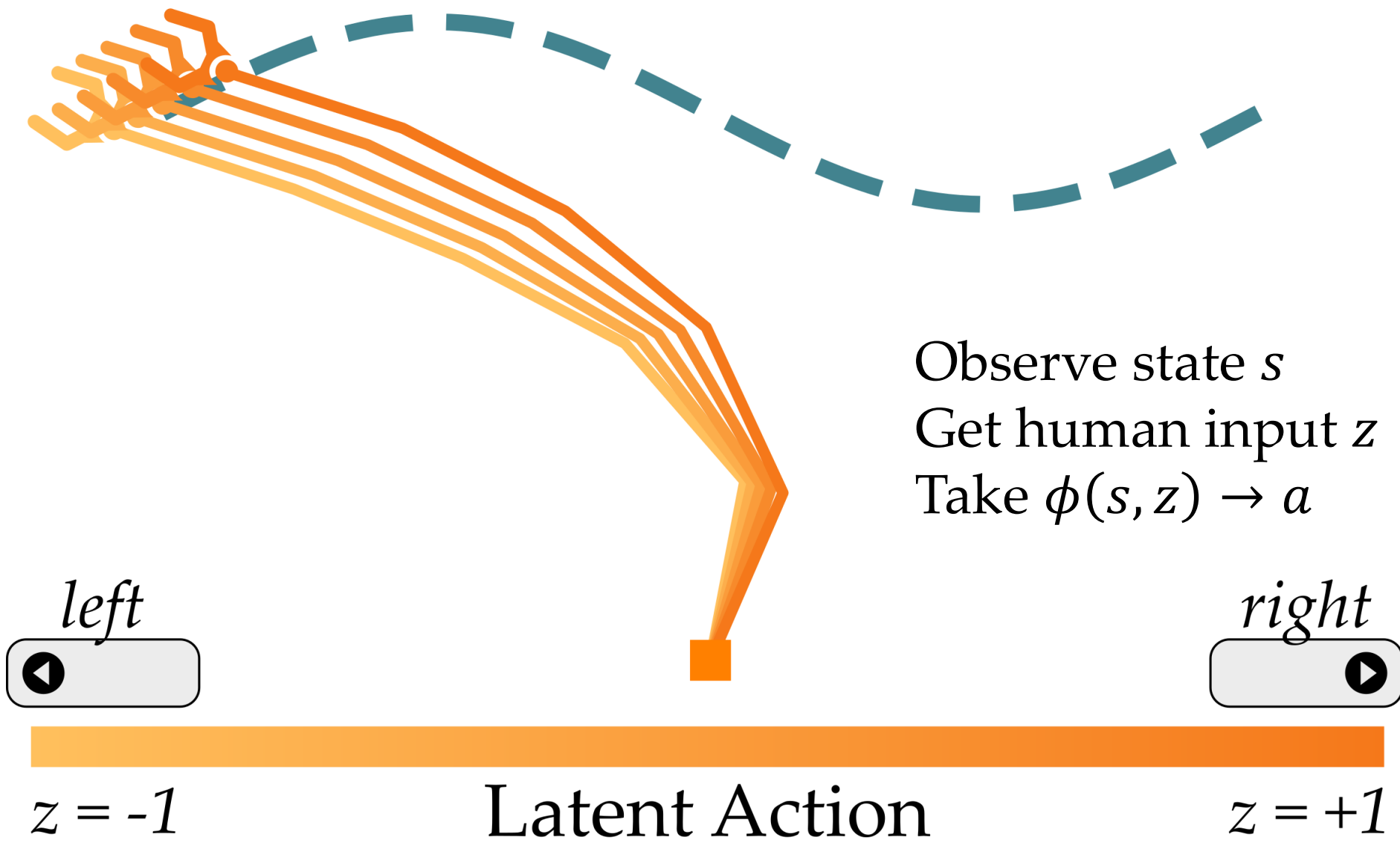
**Our idea.** We embed high-dimensional and complex tasks to low-dimensional **latent representations**. At runtime users select the latent representation with a joystick, which then maps to high-dimensional and meaningful behaviors.



---

*When robot is holding the spatula and user presses the joystick **down**, robot decodes this latent input to help automate a stirring motion*





Observe state  $s$   
Get human input  $z$   
Take  $\phi(s, z) \rightarrow a$

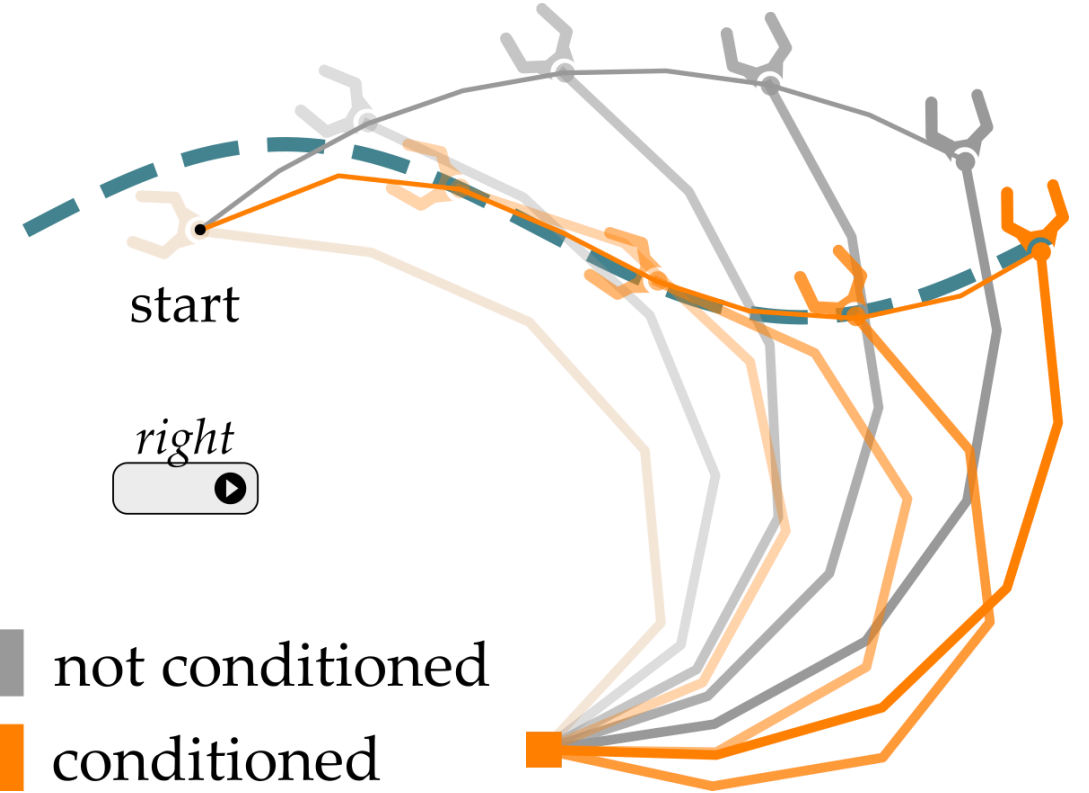
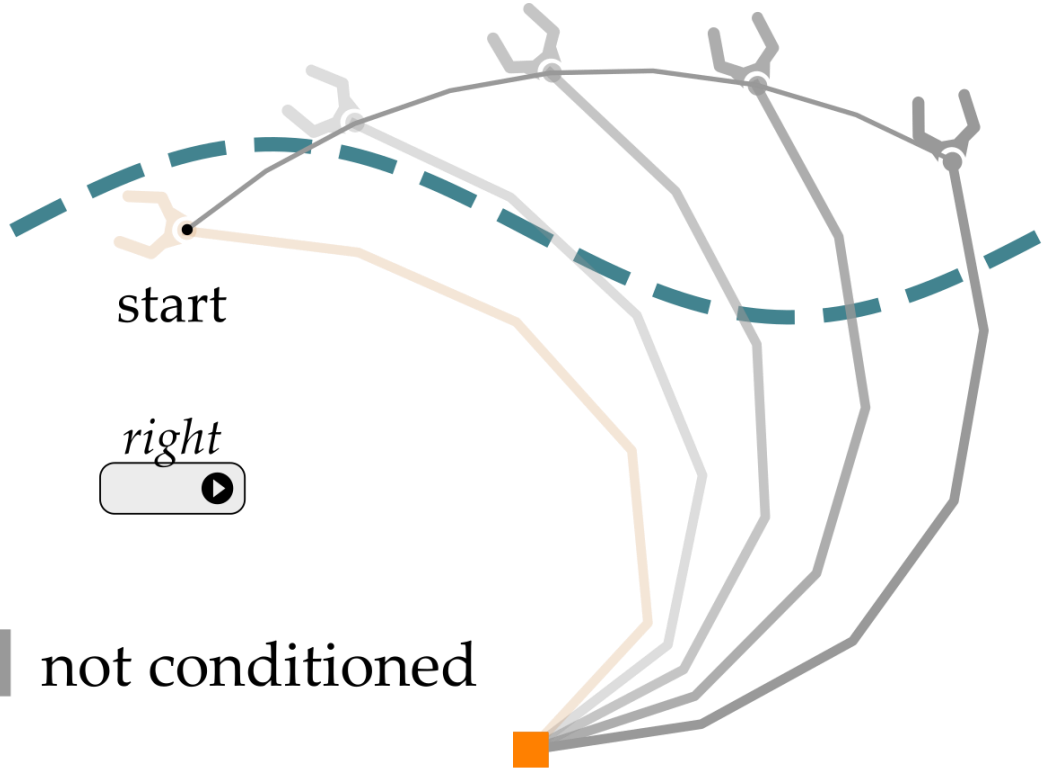
*left*  
◀

*right*  
▶

$z = -1$

Latent Action

$z = +1$



# Latent Actions

**Offline** collect dataset  $D = \{(s^1, a^1), \dots, (s^N, a^N)\}$

Initialize models:

- Encoder  $\varphi(s, a) \rightarrow z$
- Decoder  $\phi(s, z) \rightarrow a$

Train encoder and decoder to minimize loss:

$$\mathcal{L}(\theta) = \frac{1}{N} \sum_{(s,a) \in D} \|a - \phi(s, \varphi(s, a))\|^2$$

Models have weights  $\theta$

Error between actual and predicted

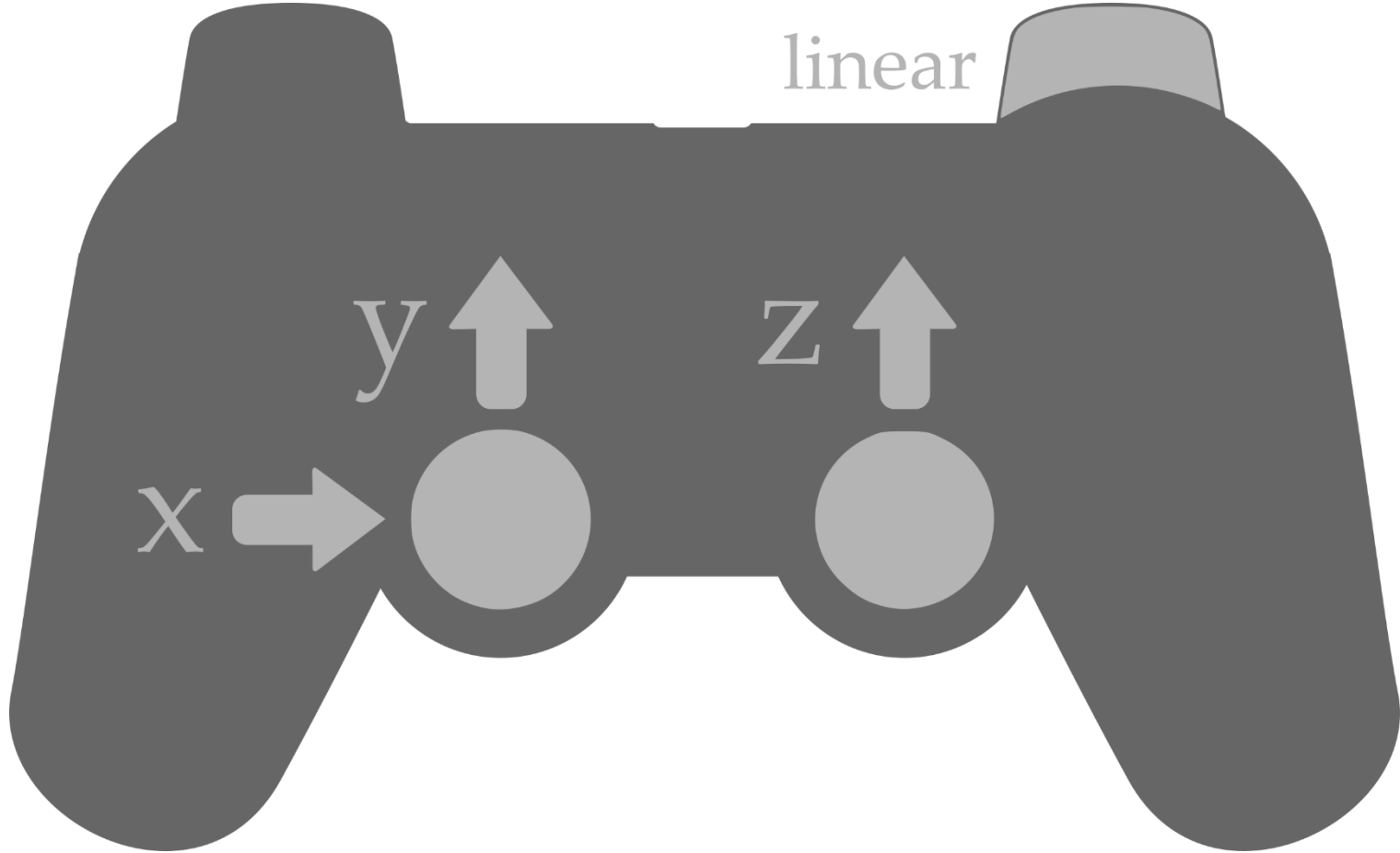
# Latent Actions

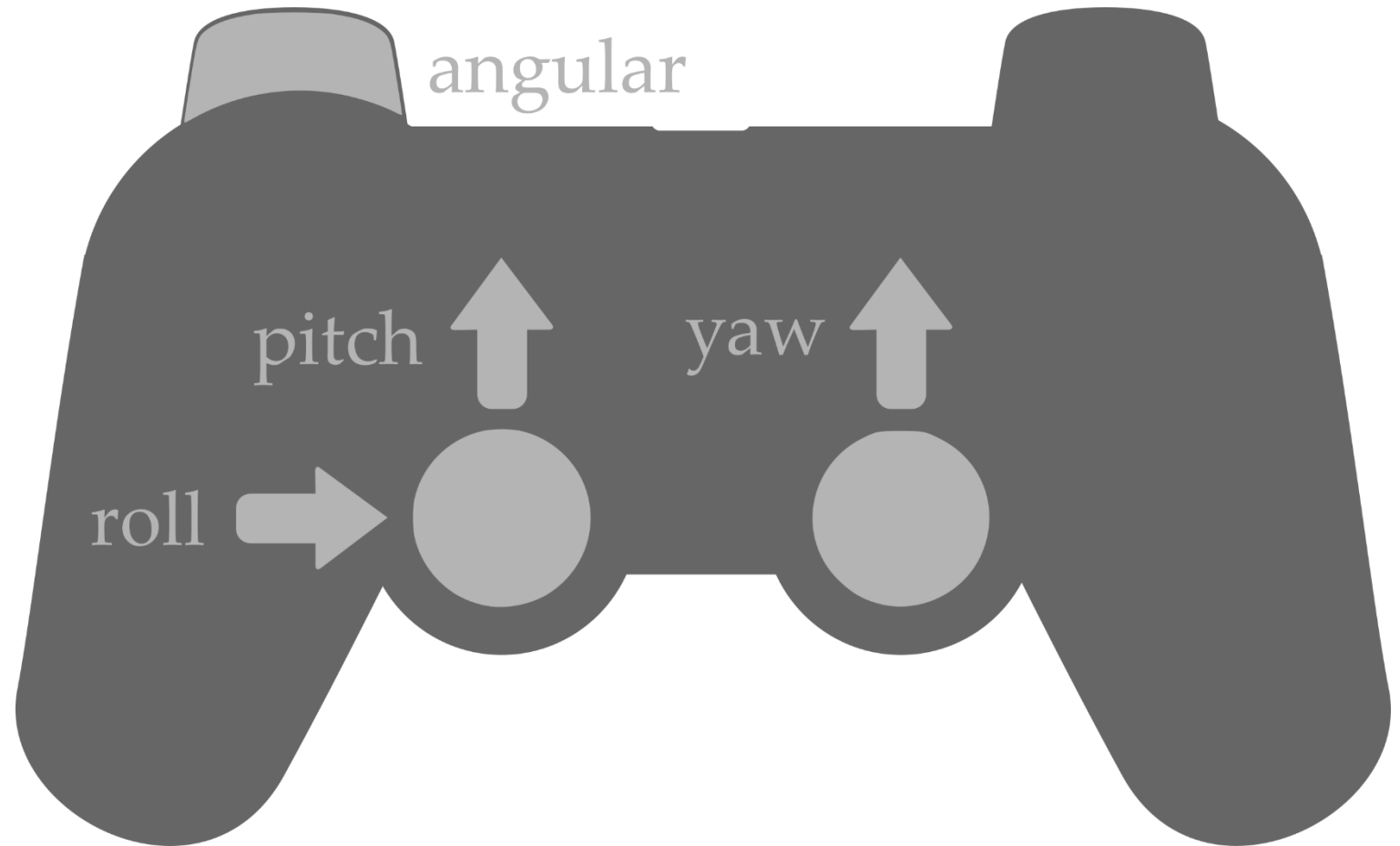
**Online** take trained decoder  $\phi(s, z) \rightarrow a$

At each timestep  $t$ :

- Observe state  $s$  and human input  $u_H$
- Treat  $z = u_H$  as the latent action
- Get decoded action  $\phi(s, z) \rightarrow a_H$
- [*Optional*] Use predict and blend to assist human
- Transition to next state

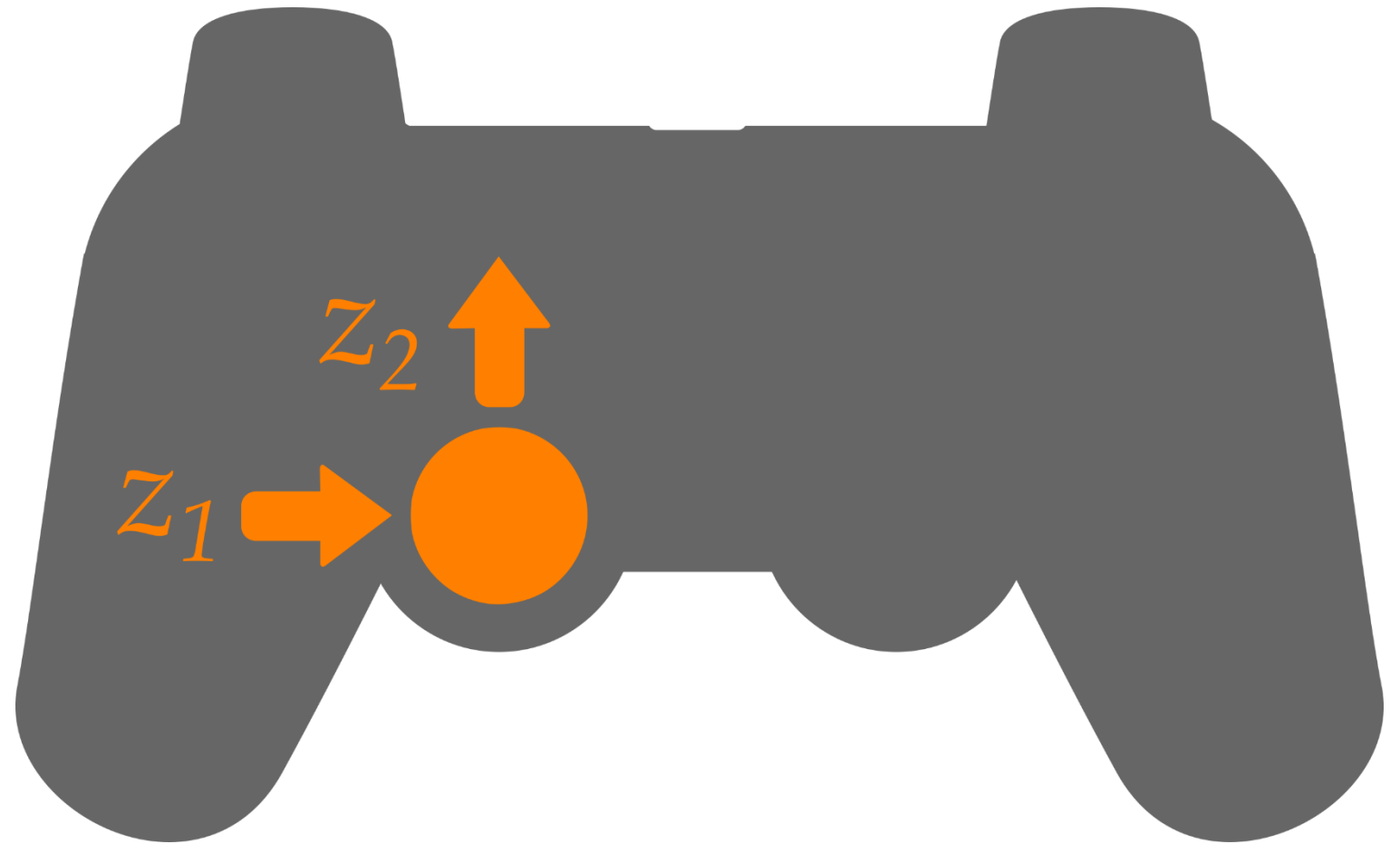
End-  
Effector







Latent  
Actions



4x Speed

(1) add eggs

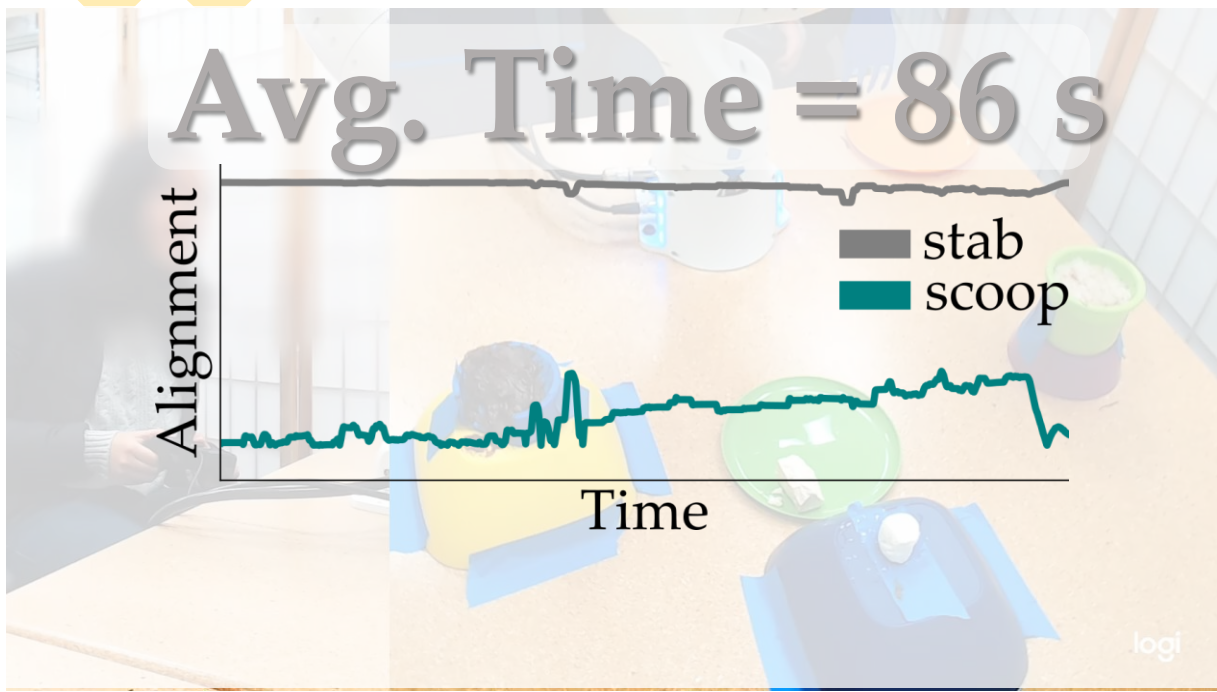


End-Effector

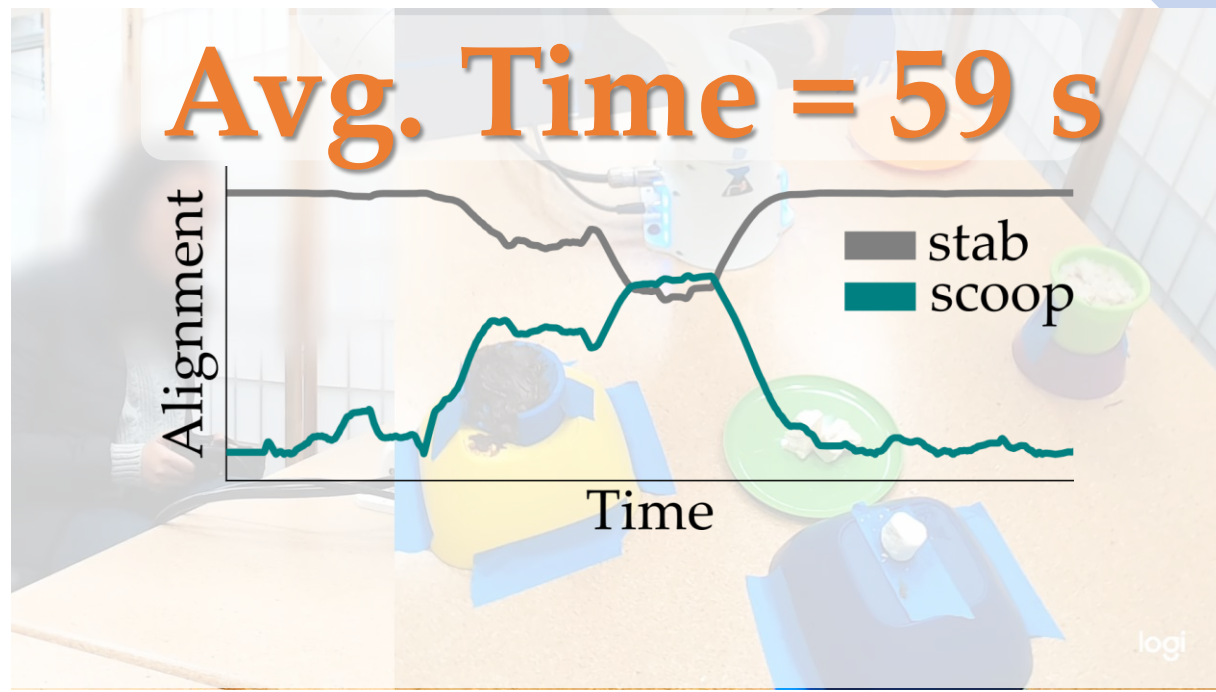
(1) add eggs



Latent Action



R



**LA + SA (ours)**



# Related Papers

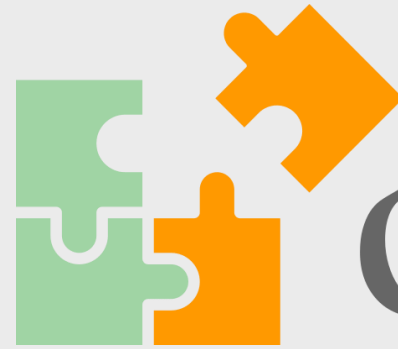
- <https://link.springer.com/article/10.1007/s10514-021-10005-w>
- <https://dl.acm.org/doi/full/10.1145/3651994>

# This Lecture

---

- Introducing shared autonomy
- One flavor of solutions: predicting goals
- Another flavor of solutions: predicting actions





collab

[collab.me.vt.edu](http://collab.me.vt.edu)